

### THE COMPARISON SOME MODELS (GAMMA, SLASHED QUASI-GAMMA, **THREE PARAMETERS QUASI GAMMA, TWO PARAMETER GAMMA-EXPONENTIAL, AND MODIFIED LOG-LOGISTIC DISTRIBUTIONS)** 0 FOR DAILY TEMPERATURE DATA J ta

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Disusun Sebagai Salah Satu Syarat untuk Memperoleh Gelar Sarjana Teknik Q Pada Program Studi Matematika Fakultas Sains dan Teknologi R a



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### The Comparison some Models (Gamma, Slashed Quasi-Gamma, three Parameters Quasi Gamma, two Parameter Gamma-Exponential, and Modified Log-Logistic Distributions) for Daily Temperature Data

Ernila Sari Gulo<sup>1</sup>, Rado Yendra<sup>2</sup>, Muhammad Marizal<sup>3</sup>, Rahmadeni<sup>4</sup>

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<b>ARTICLE INFO</b>	ABSTRACT
Published Online: 🕗	With the increase in hot temperature events in recent years, there is growing interest in measuring
02 January 2024 😐	the frequency of recurring temperature events. One of the basis for assessing the frequency of
aqi	recurrence of temperature events is the probability distribution of temperature events, therefore
an per	temperature data is needed to produce statistical modeling, especially in determining the best
ata	probability distribution. The study intended to estimate the best-fitted probability model for the
u s v	daily temperature at the Pekanbaru station in Indonesia from 2010 to 2020 using several statistical
ne ush	analyses. Five continuous probability distributions such as Gamma (GM), Slashed Quasi-Gamma
	(SQG), Three Parameters Quasi Gamma (TPQG), Two Parameter Gamma-Exponential (TPGE),
ant Ria	and Modified Log-Logistic (MLL) distributions were fitted for these tasks using the maximum
anva	likelihood technique. To determine the model's fit to the temperature data, several goodness-of-fit
a tu	tests were applied, including the graphical methos test (density plot) and Numerical criteria method
n da Nya	test (AIC, BIC, and - Log Likelihood). The GM and MLL distribution are found to be the best-
Corresponding Author:	fitted probability distribution based on goodness-of-fit tests for the daily temperature data at the
Muhammad Marizal	Pekanbaru station.

**KEYWORDS:** Gamma Distribution, Slashed Wuasi-Gamma, Three Parameters Quasi Gamma, Two Parameter Gamma-Exponential, Modified Log-Logistic, Temperature.

### 

Today's erratic temperature changes can cause great damage to us living through events such as droughts, floods and ecological disturbance because it affects human activities and the economy too. Temperature evaluation shows an important role in reviewing continuous variations in temperature falls or rise. Many different works have been carried out in response to environmental climate change, and conclusions about the critical and difficult fall and rise of ambient temperature have been drawn. Researchers are interested develop appropriate statistical methods for temperature events which provides significant help to this problem. In recent years, there have been several studies on this matter temperature events and analyzed extensively over the past two [1] [2]. Several researchers from around the world and in the country have looked into using probability distributions to analyze temperature data [3] [4] [5] [6] [7]. In this paper, our study focussed on daily temperatures in Pekanbaru city for the years 1990-2020. The purpose of this study is to quantify and

describe the behaviour of daily temperature in Pekanbaru city, Indonesia. In this study, five models distribution were tested, they are Gamma (GM), Slashed Quasi-Gamma (SQG), Three Parameters Quasi Gamma (TPOG), Two Parameter Gamma-Exponential (TPGE), and Modified Log-Logistic (MLL) distributions. When fitting a distribution model, assumed that the daily temperature follows the form of a statistical distribution. Identification of a suitable distribution is an important step in selecting best model. Comparison of the proposed distributions with existing distribution functions is done to demonstrate their suitability in describing temperature characteristics. Unknown parameter estimations were obtained with the Maximum Likelihood Method. Graphical methods and Numerical criteria such as AIC, BIC, and -1 were used to obtain the distribution which provides the best fit the temperature data. In the following section, the distributions to be used in modelling the temperature data are included.

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Gamma, Slashed Quasi-Gamma, three Parameters Quasi Gamma, two Parameters Quasi Gamma, two Parameter Gamma-Exponential, and Modified Log-Logistic Distributions) for Daily Temperature Data"

### II. DATA SET AND STUDY AREA

DIN SUSK.

Data used in this work were downloaded from the website of the Federal Office of Meteorology and Climatology of Indonesta BMKG). The original data consisted of daily temperature records from 2010 to 2020, which were provided by the BMKG of Pekanbaru city, Indonesia. The data and the histogram or characteristic wind speed are presented in Figure 1. Pekanbaru City located in Riau Province, with a tropical climate that has temperature that vary from 74 F<sup>0</sup> to 89 F<sup>0</sup>. Initial information on Temperature in the city of Pekanbaru can be seen in the descriptive statistics are presented in Table 1. The variations of temperature data that are not so large (4.58 F<sup>0</sup>) indicate that this temperature is quite stable and very good as a source of electrical energy for household purposes



Fig. F. Plot and histogram daily temperature data on Pekanbaru respectively Table Li The descriptive statistics for daily temperature data (F)

	0) (1)		
ulis	<b>Statistics</b>	Velue	
⊒:	Mean	81.85	
da	Varians	4.58	
lan	📑 Minimum	74.30	
d L	🖞 Maximum 📅	89.10	
ent	Jtk		
5	ar		

### **III. METHODOLOGY**

In this study, five models distribution were tested, they are GM, SQG, TPQG, TPGE, and MLL distributions. When fitting a distribution model, assumed that the daily temperature follows the form of a statistical distribution. Identification of a suitable distribution is an important step in selecting best model. The probability density function and log likelihood function of the distributions are given in table 2 and table 3.

 Table 2. Probability
 Density
 Function (pdf) of some distributions

hanne .	10	
The 🛱	Probability density function (pdf	)
Distributions	ar	
GM masa	$f(y) = \frac{1}{\beta^{\alpha} \Gamma(\alpha)} y^{\alpha-1} exp\left(-\frac{y}{\beta}\right),$ $y \ge 0, \ \alpha, \beta > 0$	
a		
2	lia	Muł

SQG [8]	$f(y) = \frac{q\beta^{q}y^{-(q+1)}}{\Gamma\left(\frac{1}{10}\right)}\Gamma\left(\frac{q}{\theta} + \frac{1}{10}\right)F\left(\left(\frac{y}{\beta}\right)^{\theta}, \frac{q}{\theta} + \frac{1}{10}, 1\right),$ $y > 0, \qquad q, \beta, \theta > 0$
TPQG [9]	$f(y) = \frac{2k\theta^{\alpha}y^{2k\alpha-1}exp(-\theta y^{2k})}{\Gamma(\alpha)},$ y > 0, k, $\theta, \alpha > 0$
TPGE [10]	$f(y) = \frac{k^2}{(1+k)} \left( 1 + \frac{k^{s-2}}{\Gamma(s)} y^{s-1} \right) exp(-ky),$ y > 0, k, s > 0
MLL [11]	$f(y) = \frac{a(ay)^{b-1}exp(\theta y)(b+\theta y)}{\left(1+(ay)^{b}exp(\theta y)\right)^{2}},$ y > 0, a, b, \theta > 0

### Goodness-of-Fit Tests (GOF)

The goodness-of-fit test is applied to determine the accuracy of the predicted values using the theoretical probability model. It aids in the selection of the best model from among the available distributions. For selecting the best probability distribution, several goodness-of-fit tests were applied, including the graphical methods (density plot) and numerical methods (AIC, BIC). The formula of numerical methods such as AIC and BIC are exhibited in the following Table 4

Table 3. The Log Likeliho	d of some distributions
---------------------------	-------------------------

The	Log Likelihood
Distributions	
Gamma (GM)	$l(\alpha, \beta) = \alpha - 1 \sum_{i=1}^{n} \log(y_i) - \frac{1}{\beta} \sum_{i=1}^{n} y_i$ $- n\alpha \log(\beta)$ $- n \log(\Gamma(\alpha))$
	$l(q,\beta,\theta) = c(q,\beta,\theta)$
	$-(q+1)\sum log(y_i)$
Slashed Quasi- Gamma	$+\sum_{i=1}^{n} F\left(\left(\frac{y}{\beta}\right)^{\theta}, \frac{q}{\theta} + \frac{1}{10}, 1\right)$
(SQG) [8]	where
	$c(q,\beta,\theta) = n \log(q) + nq \log(\beta) - $
	$n \log\left(\Gamma\left(\frac{1}{10}\right)\right) + n \log\left(\Gamma\left(\frac{q}{\theta} + \frac{1}{10}\right)\right)$
	and
	$F(y,\alpha,\beta) = \int_0^y \frac{\beta^{\alpha}}{\Gamma(\alpha)} y^{\alpha-1} e^{-y\beta}  dy$

Comparison some Models (Gamma, Slashed Quasi-Gamma, three Parameters Quasi Gamma, two Parameter Samma-Exponential, and Modified Log-Logistic Distributions) for Daily Temperature Data"

	$l(k, \theta, \alpha) = n \log(2) + n \log(k)$
~	$+ n\alpha \log(\theta)$
!¶hree _→ I	$(\alpha)$ + (2k $\alpha$
Darameters	
	$-1) \sum log(y_i)$
a Gamma n ta	
	$\int_{1}^{n} \sum_{k=1}^{n} 2^{k}$
The	$-\theta \sum y_i^{z_k}$
ng n ng	$\overline{i=1}$
ngi utij hal	$-n \log(\Gamma(\alpha))$
un nya nya	$l(k,s) = 2n \log(k) - n \log(1+k)$
nka	$\sum_{n=1}^{n}$
an ag	$\rightarrow$ + $\sum log(\Gamma(s))$
Parameter -	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
-Gamma a	$=$ + $\kappa^{2}$ - $\gamma^{2}$ - $\gamma^{2}$
Exponential	$-n\log(\Gamma(s))$
THE CE HOL	$\sum_{n=1}^{n}$
ga ga	$-\kappa \sum y_i$
n p	$\frac{i=1}{(a,b,q) - nb\log(q)}$
ka en ya	$\frac{l(a,b,b)}{l(a,b,b)} = \frac{l(b,b)}{l(b,b)} \frac{l(b,b)}{l(b,b)} + \frac{l(b,b)}{l(b,b)} \frac{l(b,b)}{l(b,b)} \frac{l(b,b)}{l(b,b)} + \frac{l(b,b)}{l(b,b)} \frac{l(b,b)}{$
rya did yau	
a tu lika eb	$=$ -1) $\sum log(y_i)$
an, ag	
ini jar	
Modified	$+\theta \sum y_i$
Log-Logistic	$\sum_{i=1}^{n}$
((MELL)) []]	$\sum_{n=1}^{n}$
ner pe ska	$+ \sum_{i} log(b+y_i)$
uh B R	$\overline{i=1}_{n}$
intu liss ka	$2\sum_{l=1}^{n} log(1)$
um an 1.	$=2 \sum log(1)$
kar ka	i=1 + $(ay)^{b}eyn(Ay)$
n d nya	+(uy) exp(0y)
0)	

### VI. RESULT AND DISCUSSION

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In this section, we analyze a daily temperature data set to demonstrate the performance of the GM, SQG, TPQG, TPEG and MLL distributions in practice. The fitting of that distributions was considered using data from the period between 2010 and 2020. Computed parameter values of different probability density function used for the BMKG Pekanbaru stations are presented in Table 5.

 Table 4. The formulas of numerical criteria for model

 evaluation

Nun	nerical Crite	ria	Formula
AIC	an	V C	-2l + 2q
BIC	Kr.	f	$-2l + q \log(n)$
le log	g fikelihood,	q = Num	ber of parameters, $n =$ number of
data	ata	lt	
liau	u ti	an	

 Table
 S.
 Computed parameter values of different probability density functions

	GМ	SQG	TPQG	TPGE	MLL
α	0.06		-	-	-
ß	1320.99	- 2	-	-	-
$\boldsymbol{q}$	- na	55.61	-	-	-
ß	- sa	82.37	-	-	-
	a	5			
3	р.	ia			Muhai
		F			

$\boldsymbol{\theta}$	-	419.77	-	-	-
k	-	-	1.73	-	-
$\boldsymbol{\theta}$	-	-	1.18 x 10 <sup>-6</sup>	-	-
α	-	-	4.93	-	-
k	-	-	-	0.90	-
S	-	-	-	74.27	-
a	-	-	-	-	1.05 x 10 <sup>-8</sup>
b	-	-	-	-	4.42

On the graphical presentation of modelling of the daily temperature data, the density function curve for GM, SQG, TPQG, TPEG and MLL distributions models are seen in Figure 2, 3, 4, 5 and 6 are respectively. When the density functions (pdf) are examined, it was determined that some distributions have yield similar results. From this figure GM and MLL distributions model is able to provide a good result for daily temperature data. However, instead of graphical evaluation, Table 6 provides a more meaningful comparison using AIC, BIC, and -1 values.



Fig 5. Fitted pdf plots of TPEG distribution

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parison some Models (Gamma, Slashed Quasi-Gamma, three Parameters Quasi Gamma, two Parameter amma-Exponential, and Modified Log-Logistic Distributions) for Daily Temperature Data"



Fig 6. Fitted pdf plots of MLL distribution lidak umun a

Table 6 includes AIC, BIC and - l values test statistics values of the goodness of fit test for the fitness of daily temperature data based on Maximum Likelihood Estimators for GM, SQG, TPQG, TPEG, and MML distributions. According to these results, the lowest AIC, BIC and - l value are obtained for GM and MML distributions. As a conclusion, it is seen that GM and MML distribution provides better modelling in terms of Numerical criteria

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Table 4 AIC, BIC, and – Log Likelihood (1) function values\_

2 0	Q E				
n c	GM	SQG	TPQG	TPEG	MLL
ĀI	16674.8	17049.3	25351.1	29314.3	16754.1
So S	len oa	0	9	5	6
₿I5	16687.3	17068.0	25369.9	29335.0	16772.9
C a	one and	4	4	9	0
코1고	8335.43	8521.65	12672.6	14655.1	8374.07
au	is a			8	9
~					

### **V. CONCEUSSION**

In the present article, a comparison of distribution models has been undertaken for describing temperature of Pekanbaru stations. Common conventional density GM and extended pdf along with four proposed density function such as SQG, TPQG, TPEG and MLL are used for temperature modeling. It is shown that extended density such as SQG, TPQG and TPEG is inadequate, hence, conventional density functions GM and the extended density MLL are used to model the observed temperature distributions better. Results show clearly that proposed GM and MLL provide viable alternative to other pdf in describing temperature regimes.

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